

1 Rapid frequency modulation in a resonant system: aerial perturbation
2 recovery in hawkmoths – Supplemental Information

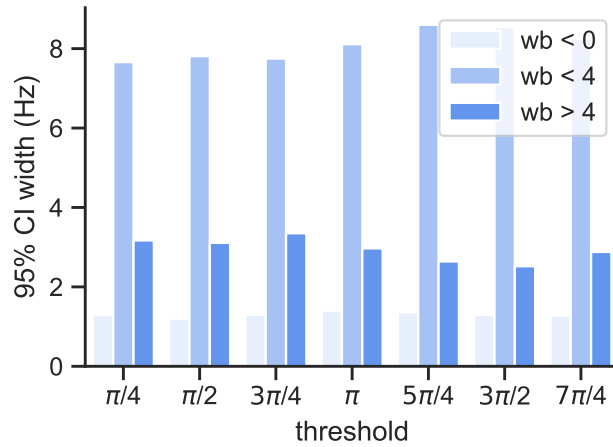
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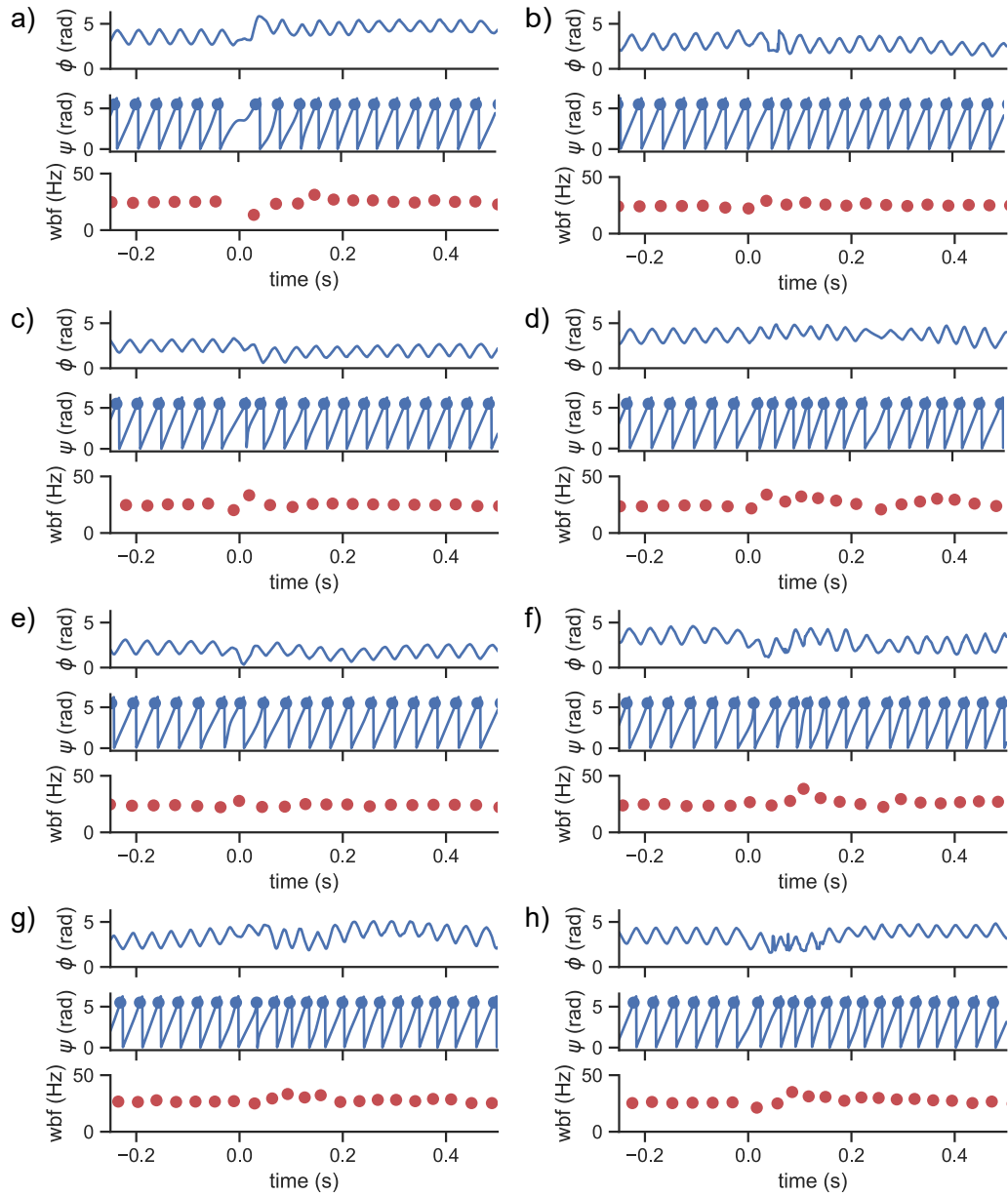
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11 Supplemental Figure S1: Our conclusions of wingbeat frequency modulation are robust to our choice of phase
12 threshold. We used a threshold approach to calculating wingbeat frequency from ψ . Regardless of the threshold,
13 we found that the 95% quantile width is greatest for the four wingstrokes immediately following the perturbation,
14 followed by the subsequent four wingstrokes. The four wingstrokes pre-perturbation have consistently the smallest
15 95% quantile width.



16 Supplemental Figure S2: a-h) Wing angle (ϕ), instantaneous phase (ψ) and wingbeat frequency (wbf) for the first
 17 trial for each of the eight moths used in this manuscript.

18 **Supplemental Movie Captions**

19 Supplemental Movie S1: Rear view movie of a representative perturbation. Video is recorded at 2000 fps and slowed
20 20x.

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23 Supplemental Movie S2: Top-down movie of a representative perturbation. Video has been background subtracted
24 and points labeled via DeepLabCut superimposed.

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27 Supplemental Movie S3: Video overview of the instantaneous phase method for determining changes in driving
28 frequency.